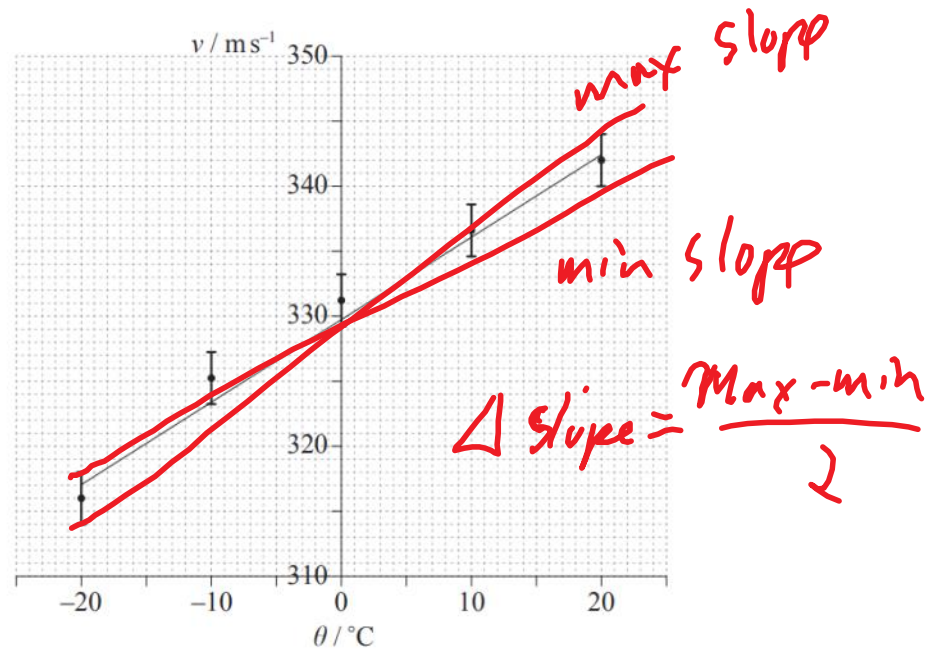


SECTION A

Answer **all** questions. Write your answers in the boxes provided.

1. The speed of sound in air, v , was measured at temperatures near 0°C . The graph shows the data and the line of best-fit. The error bars for temperature are too small to be shown.



A student suggests that the speed of sound v is related to the temperature θ in degrees Celsius by the equation

$$v = a + b\theta$$

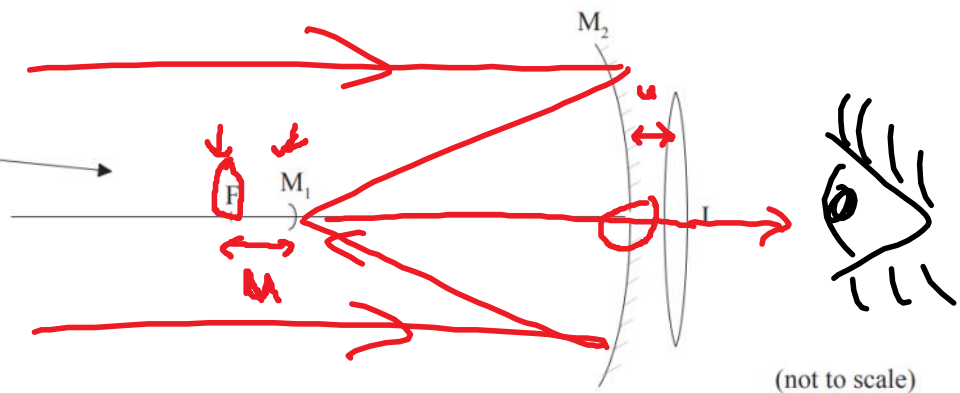
$$-Q_{\text{metal}} = Q_{\text{water}}$$

$$-Q_{\text{met}} + Q_{\text{extra}} = Q_{\text{water}}$$

$$-m_w c_w (T_f - T_i) + Q = m_w c_w (T_f - T_w)$$

option

8. (a) The diagram shows a Cassegrain reflecting telescope consisting of a small diverging mirror M_1 , a large converging mirror M_2 , and a converging lens L . The focal point of M_2 is at F .



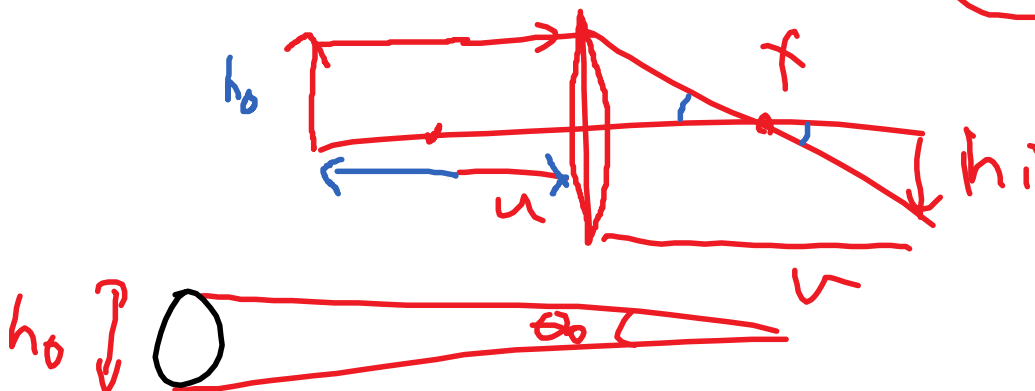
$m = \frac{h_i}{h_o} = \frac{\theta_i}{\theta_o}$
 $\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$
 $d_o \quad d_i$

The telescope is used to view a planet. The diameter of the planet subtends an angle of 1.40×10^{-4} rad at M_2 . The focal length of M_2 is 9.50 m.

- (i) Show that the diameter of the image of the planet that would be formed by M_2 alone is 1.33 mm. [3]

$\theta_o = 1.4 \times 10^{-4} \text{ rad} \quad f = 9.50 \text{ m}$
 if u is very big $f \approx v$

$D_i = -f\theta_o \approx -9.50 \text{ m} \times 1.4 \times 10^{-4}$
 $\approx -1.33 \text{ mm}$



$$\frac{1}{f} = \frac{1}{v} + \frac{1}{u}$$

$$m = \frac{h_i}{h_o} = -\frac{v}{u}$$

$$M = \frac{\theta_i}{\theta_o}$$



$$\frac{h_o}{u}$$

~~h_o~~

$$\frac{h_i}{h_o} = -\frac{v}{u}$$

$$h_i = -v \left(\frac{h_o}{u} \right)$$

$$h_i = -v\theta_o$$

(Option C, question 8 continued)

- (ii) M_1 is at a distance of 8.57 m from the aperture of M_2 . The image in (a)(i) now serves as a virtual object for M_1 . A real image is formed at the opening of M_2 . Show that the diameter of this image is 12.0 mm. [3]

$$v = 8.57 \text{ m} \quad D_o = 12.0 \text{ mm}$$

$$\frac{D_i}{D_o} = \frac{-v}{u} \quad D_i = -D_o \frac{v}{u} = \frac{1.33 \text{ mm} \times 8.57 \text{ m}}{(9.50 \text{ m} - 8.57 \text{ m})} = 12.0 \text{ mm}$$

- (iii) The real image in (a)(ii) is now viewed by L of focal length 98.0 mm. The final image of the planet is formed at infinity. Calculate the overall magnification of the telescope. [3]

$$\frac{1}{f} = \frac{1}{u} + \frac{1}{v}$$

$$M = ? \quad v = \infty \quad u = f$$

$$M = \frac{\theta_i}{\theta_o} = \frac{12 \text{ mm}}{98 \text{ mm}} = 1.4 \times 10^{-4} \text{ rad}$$

(Option C continues on the following page)